

novelty - Convex Optimization & Euclidean Distance Geometry

- p.120 *Conic independence* is introduced as a natural extension to linear and affine independence; a new tool in convex analysis most useful for manipulation of cones.
- p.148 Arcane theorems of alternative *generalized inequality* are simply derived from cone *membership relations*; generalizations of *Farkas' lemma* translated to the geometry of convex cones.
- p.229 We present an arguably good 3-dimensional polyhedral analogue, to the isomorphically 6-dimensional positive semidefinite cone, as an aid to understand semidefinite programming.
- p.256, p.273 We show how to constrain rank in the form $\text{rank } G \leq \rho$ and cardinality in the form $\text{card } x \leq k$. We show how to transform a rank constrained problem to a rank-1 problem.
- p.321, p.325 *Kissing-number of sphere packing* (first solved by Isaac Newton) and *trilateration* or *localization* are shown to be convex optimization problems.
- p.336 We show how to elegantly include *torsion* or *dihedral angle* constraints into the *molecular conformation problem*.
- p.367 Geometrical proof: *Schoenberg criterion* for a Euclidean distance matrix.
- p.385 We experimentally demonstrate a conjecture of Borg & Groenen by reconstructing a map of the USA using only ordinal (comparative) distance information.
- p.6, p.403 There is an equality, relating the convex cone of Euclidean distance matrices to the positive semidefinite cone, apparently overlooked in the literature; an equality between two large convex Euclidean bodies.
- p.447 The *Schoenberg criterion* for a Euclidean distance matrix is revealed to be a discretized *membership relation* (or *dual generalized inequalities*) between the EDM cone and its dual.